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Specification and Verification of Reconfiguration Protocols in Grid Component Systems

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Abstract

In this work we present an approach for the formal specification and verification of the reconfiguration protocols in Grid component systems. We consider Fractal, a modular and extensible component model. As a specification tool we invoke a specific temporal language, separated clausal normal form, which has been shown to be capable of expressing any ECTL\(^+\) expression, thus, we are able to express the complex fairness properties of a component system. The structure of the normal enables us to directly apply the deductive verification technique, temporal resolution defined in the framework of branching-time temporal logic.

1 Introduction

There are two approaches to building long-lived and flexible Grid systems: exhaustive and generic. The former approach provides rich systems satisfying every service request from applications but consequently its implementation suffers from very high complexity. In the latter approach, we represent only the basic set of services (minimal and essential) and thus overcome the complexity of the exhaustive approach. However, to achieve the full functionality of the system, we must make this lightweight core platform reconfigurable and expandable. One of the possible solutions here is to identify and describe the basic set of features of the component model and to consider any other functions as pluggable components [31] which can be brought on-line whenever necessary [27].

Establishing the theoretical foundations of the generic processes involved in designing and functioning of such Grid systems is highly important. A significant part of this research lies in the area of formal specification and verification of the core component model and the properties of the desired Grid systems.

Among various approaches to representing a component model we pay specific attention to the Fractal component model [18]. The advantage of the Fractal framework is that it defines the structure of the components, gives a basic classification of components, and has the mathematical foundations, e.g., the Kell calculus [8]. The Fractal specification defines the basic (non-functional) controls which should be defined especially to enable dynamic reconfiguration of components, and a number of constraints on the interplay between functional and non-functional operations. The
reconfiguration is obtained by triggering appropriate actions on specific types of the components’ interfaces. These explicit dynamic properties of the Fractal component model are particularly suitable for Grid systems and environments. In this work we focus on predefined categories of reconfigurations and also on proving properties of these reconfigurations.

Given a formal specification of a distributed system there are two major approaches to formal verification of this specification: algorithmic and deductive [29]. While the algorithmic approach is fully automated, as in the case of model checking, its application, in general, is restricted to finite state systems. On the other hand, methods of the second, deductive approach, can handle arbitrary systems providing uniform proofs. To the best of our knowledge, the only technique currently used in the verification of distributed hierarchical components is model checking. We started from the point of view developed in [5, 4]. The basic blocks in a component model (called primitive components in the sequel) are provided by the programmer as black boxes, usually in a programming language of their choice. The starting point for model checking of components is the specification of the primitives, either by the programmer, or by static analysis of the source code. The research in [5] shows how to generate the behaviour for asynchronous systems of components from these basic blocks in the form of a pLTS (parameterized labeled transition system). This enables the verification of system properties by employing model checking techniques.

In a similar way, we can provide the formal framework for the components in a specific branching-time temporal logic, or SNF_{CTL} (Separated Normal Form for Computation Tree Logic) [15], and then directly apply temporal resolution as a deductive verification tool.

CTL type branching-time temporal logics play a significant role in potential applications such as the specification and verification of concurrent and distributed systems [21]. In particular, two combinations of future time temporal operators $\diamond$ (‘sometimes’) and $\Box$ (‘always’), are useful in expressing fairness [20]: $\diamond \Box p$ ($p$ is true along the path of the computation except possibly for some finite initial interval of it) and $\Box \diamond p$ ($p$ is true along the computation path at infinitely many moments of time). It has been shown that SNF_{CTL} can express these simple fairness constraints and their Boolean combinations [11, 12]. Furthermore, a clausal resolution over the set of SNF_{CTL} clauses has been defined [10, 11]. Recently, the search strategies for this method were presented in [13].

These developments allow us to reason about the configuration/(re)configuration protocols of a Grid component model on behalf of the following formal framework:

$$FCM \rightarrow SNF_{ctl}(FCM) \rightarrow BTR$$

Here we suggest the translation of the Fractal component model (FCM) into the SNF_{ctl}(FCM), the SNF_{ctl} based formal specification of FCM, and to apply the ‘branching temporal resolution’ method (BTR), the temporal resolution technique defined over the set of SNF_{ctl} clauses.

In this paper we show how to extract the desired SNF_{ctl} based temporal specification for a given component model. The output system would have an intelligent verification engine strengthened with the corresponding search techniques as well as with the possibility of invoking powerful refinement methods developed for the resolution in the classical setting.

Moreover, we also derive the problem structure to achieve even greater level of intelligence of the developed system by invoking the erotetic framework [16]. The Inferential Erotetic Logic (IEL) [32, 35] is a powerful tool in the area of analyzing and modelling such components of intelligent activity as planning, problem solving, and searching for information in massive data/knowledge bases [33]. Important developments within the framework of IEL are Erotetic Search Scenarios (ESS) [34] and Socratic Proofs (SP) [36]. ESS is based on the idea of providing conditional instructions for solving an initial problem, informing us which questions should be asked and when they should be asked. Moreover, an erotetic search scenario shows where to go if a direct answer to a query appears to be acceptable and does so with respect to any direct answer to each query. SP is a very specific technique, which reduces the complexity of standard problem-solving methods by using pure questioning only.

The structure of the paper is as follows. In Section 2 we outline the Fractal approach to a component model and its reconfiguration. In Section 3 we present SNF_{ctl} based formal specification technique for a Fractal component model. Here we first, discuss main approaches to verification in Subsection 3.1, then we review the syntax and semantics of the specification language, SNF_{ctl} in Subsection 3.2, and finally, in Subsection 3.4 we apply SNF_{ctl} to specify a concrete example. Next, in Section 4, we apply the clausal resolution technique as a verification tool. Thus, in Subsection 4.1 we review the temporal resolution and in Subsection 4.2 we apply this method to the verification of the component model (previously specified in Section 3). Finally, in Section 5, we draw conclusions and discuss future work.
2 Reconfiguration Scenario for Component Model

2.1 Component Model

Fractal is a modular and extensible component model. The Fractal specification defines a set of notions characterizing this model, an API (Application Program Interface), and an ADL (Architecture Description Language).

Components are characterized by their content and the membrane. The content of a component can be hidden (in which case it is simply a black box) or it can be constituted by a system of some other components (sub-components). In the former case we would call a component primitive while the latter case represents a composite component. The membrane, or controller, controls the component. Controllers address non-functional aspects of the component.

Fractal is a multi-level specifications. Depending on their conformance level, Fractal components can feature introspection and/or configuration. The control interfaces are used in the Fractal model to allow configuration (reconfiguration), and are defined as non functional. On the other hand, the functional interfaces of a component are associated with its functionalities. A functional interface can provide the required functionalities and we call it the server interface. Alternatively, a client interface requires some other functionalities.

Component interfaces are linked together by bindings. In this paper, we will only consider primitive bindings that are simple bindings transmitting invocations from the client interface to the connected server interface.

There are four controllers that have been already defined in Fractal (but others may be user-defined depending on the needs of the model):

- The attribute controller is used to configure a property within a component, when there is no need to take into consideration bindings of interfaces.
- The binding controller is used when the attribute controller is not applicable and actual binding/unbinding of interfaces is required.
- The content controller can be used to retrieve the representation of the sub components and add or remove them accordingly; note that if a sub component is shared by one or more other components, the scenario must be defined so that also these other components are taken into consideration.
- The life cycle controller allows to start and stop a component, it is used for dynamic reconfiguration so that all other controls can be applied safely to the component while the component is not in execution.

These are the basic controls which should be defined especially to be able to have dynamic reconfiguration of components.

The Fractal specification defines a number of constraints on the interplay between functional and non-functional operations:

- Content and binding control operations are only possible when the component is stopped.
- When stopped, a component does not emit invocations and must accept invocations through control interfaces; whether or not an invocation to a functional interface is possible is undefined.

2.2 Configuration/Reconfiguration Scenario

In general, the initial configuration of a Fractal component is given by the description of the component using Fractal ADL.

From this first state, reconfiguration is obtained by triggering appropriate actions on the the life-cycle, the binding, and the content control interfaces. A reconfiguration can be triggered by any component that has a reference to a correct non-functional interface.

In this work we focus on predefined categories of reconfigurations and on proving properties on these reconfiguration. As far as the reconfiguration is concerned we use the classical assumption that replacing a component by a similar one is safe for the system.
3 Specification of the Scenario in Temporal Logic Framework

3.1 Formal Specification and Verification of Components

We distinguish the specification of the primitives and of the composite component. The primitives are specified as a black box, usually in a programming language of our choice. The component composition is specified using Fractal ADL (Fractal Architecture Definition Language), and from this specifications it is possible to extract the bindings between interfaces of subcomponents and the controllers of the component itself.

3.2 Specification Language: Normal Form for ECTL+$^+$

As our specification tool we utilize the language of a normal form, SNF$_{\text{CTL}}$, developed for a number of branching-time logics, CTL [9, 15], ECTL [11] and ECTL+$^+$ [12]. The SNF$_{\text{CTL}}$ language is based upon the extended set of classical logic operators $\land$, $\lor$, $\Rightarrow$, $\neg$, the set of future time temporal operators $\Box$ (always), $\Diamond$ (sometime), $\bigcirc$ (next time) and path quantifiers $A$ (on all future paths) and $E$ (on some future path).

We precede the presentation of the SNF$_{\text{CTL}}$ language by the introduction of notations of tree structures, the underlying structures of time assumed for the logic under consideration.

Definition 1 (Tree) A tree, $T$, is a pair $(S, R)$, where $S$ is a set of states and $R \subseteq S \times S$ is a relation between states of $S$ such that

- $s_0 \in S$ is a unique root node, i.e. there is no state $s_i \in S$ such that $R(s_i, s_0)$;
- for every $s_i \in S$ there exists $s_j \in S$ such that $R(s_i, s_j)$;
- for every $s_i, s_j, s_k \in S$, if $R(s_i, s_k)$ and $R(s_j, s_k)$ then $s_i = s_j$.

A path, $\chi_{s_i}$ is a sequence of states $s_i, s_{i+1}, s_{i+2} \ldots$ such that for all $j \geq i$, $(s_j, s_{j+1}) \in R$. A path $\chi_{s_0}$ is called a fullpath. Let $X$ be a family of all fullpaths of $T$. Given a path $\chi_{s_i}$ and a state $s_j \in \chi_{s_i}$, $(i < j)$ we term a finite subsequence $[s_i, s_j] = s_i, s_{i+1}, \ldots, s_j$ of $\chi_{s_i}$ a prefix of a path $\chi_{s_i}$, and an infinite sub-sequence $s_j, s_{j+1}, s_{j+2}, \ldots$ of $\chi_{s_i}$ a suffix of a path $\chi_{s_i}$ abbreviated $Suf(\chi_{s_i}, s_j)$.

Definition 2 (Countable $\omega$-tree) A countable $\omega$-tree, $T_\omega$, is a tree $(S, R)$ with the family of all fullpaths, $X$, which satisfies the following conditions:

- each fullpath $\chi \in X$ is isomorphic to natural numbers;
- every state $s_i \in S$ has a countable number of successors.

Definition 3 (Branching degree of a state) The number of immediate successors of a state $s_i \in S$ in a tree $(S, R)$ is called the branching degree of $s_i$.

Since underlying models are countable $\omega$ trees, a state in such a model can have an infinite number of successor states. However, following [24] (Theorem 3.2), if a formula $F$ is satisfiable in a CTL+$^+$ (hence SNF$_{\text{CTL}}$) model then it has a (finite) model, where each state has a branching degree $\leq |F|$ (where $\leq |F|$ is the length of $F$). More precisely, given an interpretation $\langle M, s_0 \rangle$ for a set, $G$, of SNF$_{\text{CTL}}$ clauses, there exists a special interpretation $\langle M', \lambda \rangle$ (where $\lambda$ is the number of existential path quantifiers in $G$, such that $G$ is satisfied in $\langle M, s_0 \rangle$ iff $G$ is satisfied in $\langle M', \lambda \rangle$. As shown in [10, 11], this justifies our interpretation of the labeled SNF$_{\text{CTL}}$, clauses given below (see section 3.3).

Closure properties of ECTL+$^+$ models. When trees are considered as models for distributed systems, paths through a tree are viewed as computations. The natural requirements for such models would be suffix and fusion closures. Following [20], the former means that every suffix of a path is itself a path. The latter requires that a system, following the prefix of a computation $\gamma$, at any point $s_j \in \gamma$, is able to follow any computation $\pi_{s_j}$ originating from $s_j$.

Finally, we might require that “if a system can follow a path arbitrarily long, then it can be followed forever”. This requirement is known as the limit closure property, as defined in [20]. More specifically, it means that for any fullpath $\gamma_{s_0}$ and any paths $\pi_{s_j}, \varphi_{s_k}, \ldots$ such that $\gamma_{s_0}$ has the prefix $[s_0, s_j]$, $\pi_{s_j}$ has the prefix $[s_j, s_k]$, $\varphi_{s_k}$ has the
where clauses where each of the

Definition 4 (Separated Normal Form SNF

\( \text{CTL} \)

moment of time' with the intended meaning that it is true only at the initial moment of time).

indices makes paths explicit and is related to the branching factor of the canonical model.

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associated with

\( \langle \), it satisfies all three closure properties, i.e. it is suf ffix, fusion and limit closed.

prefix \([s_k, s_l]_\text{ind}\), etc, and \(0 < j < k < l\), the following holds (see Figure 1): there exists an infinite path \(\alpha_{s_0}\) that is a limit of the prefixes \([s_0, s_j], [s_j, s_k], [s_k, s_l]_\text{ind}\), . . .

In our definition of an SNF\(_\text{CTL}\) model structure \(\mathcal{M}\) the set of fullpaths \(X\) is \(R\)-generable. Therefore, following [20], it satisfies all three closure properties, i.e. it is suffix, fusion and limit closed.

Now we are ready to define the formal syntax and semantics for SNF\(_\text{CTL}\). A set of SNF\(_\text{CTL}\) clauses is interpreted in a structure \(\mathcal{M} = \langle S, R, s_0, X, L \rangle\), where \((S, R)\) is a countable \(\omega\) tree with a root \(s_0\), \(X\) is a set of all fullpaths and \(L\) is an interpretation function mapping atomic propositional symbols to truth values at each state and the following conditions are satisfied:

- \(X\) is \(R\)-generable [20], i.e. for every state \(s_i \in S\), there exists \(\chi_j \in X\) such that \(s_i \in \chi_j\), and for every sequence \(\chi_j = s_0, s_1, s_2, \ldots\), the following is true: \(\chi_j \in X\) if, and only if, for every \(i, R(s_i, s_{i+1})\);

- a tree \((S, R)\) is of at most countable branching.

Syntax. First, we fix a countable set, \(Prop = x, y, z, \ldots\), of atomic propositions. The core idea of SNF\(_\text{CTL}\) is to represent temporal information in the following three types of constraints. Initial constraints represent information relevant to the initial moment of time, the root of the computation tree. Step constraints indicate what will happen at the successor state(s) given that some conditions are satisfied ‘now’. Finally, Sometimes constraints keep track on any eventuality, again, given that some conditions are satisfied ‘now’. Additionally, to enable sound reasoning within a specific path context during the verification, we incorporate indices.

Indices. The language for indices is based on the set of terms

\[
\text{IND} = \{ (f), (g), (h), \langle \text{LC}(f) \rangle, \langle \text{LC}(g) \rangle, \langle \text{LC}(h) \rangle \ldots \}
\]

where \(f, g, h \ldots\) denote constants. Thus, \(E A(f, g)\) will be taken to mean that \(A\) holds on some path labelled as \((f)\). A designated type of indices in SNF\(_\text{CTL}\) are indices of the type \(\langle \text{LC}(\text{ind}) \rangle\) which represent a limit closure of prefixes associated with \(\langle \text{ind} \rangle\). All Formulae of SNF\(_\text{CTL}\) of the type \(P \Rightarrow E \Box Q\) or \(P \Rightarrow E \Diamond Q\), where \(Q\) is a purely classical expression, are labeled with some index. As previously mentioned, the labelling of the clauses of the normal form by indices makes paths explicit and is related to the branching factor of the canonical model.

Additionally, we introduce classically defined constants \text{true} and \text{false}, and a new operator, \(\text{start}\) (‘at the initial moment of time’ with the intended meaning that it is true only at the initial moment of time).

Definition 4 (Separated Normal Form SNF\(_\text{CTL}\)) A set of SNF\(_\text{CTL}\) clauses is a set of Formulae \(\begin{array}{c} A \square \left[ \bigwedge \left(P_j \Rightarrow F_j\right) \right] \\
\end{array}\)

where each of the clauses \(P_j \Rightarrow F_j\) is further restricted as below, each \(\alpha_j, \alpha_p, \alpha_t, \alpha_v, \beta_i, \beta_m, \beta_r\), or \(\gamma\) is a literal, \text{true} or \text{false} and \((\text{ind}) \in \text{IND}\) is some index.

- \(\text{start}\) \(\Rightarrow \bigvee_{i=1}^{k} \beta_i\) an initial clause
- \(\bigwedge_{j=1}^{l} \alpha_j\) \(\Rightarrow A \Box \left[ \bigvee_{m=1}^{n} \beta_m \right]\) an A step clause
- \(\bigwedge_{p=1}^{q} \alpha_p\) \(\Rightarrow E \Box \left[ \bigvee_{r=1}^{s} \beta_r \right]_{\langle \text{ind} \rangle}\) an E step clause
- \(\bigwedge_{t=1}^{u} \alpha_t\) \(\Rightarrow A \Diamond \gamma\) an A sometime clause
- \(\bigwedge_{v=1}^{w} \alpha_v\) \(\Rightarrow E \Diamond \gamma_{\langle \text{LC}(\text{ind}) \rangle}\) an E sometime clause
3.3 Interpreting SNF<sub>CTL</sub>.

Below we define a relation $\models$ which evaluates the SNF<sub>CTL</sub> clauses at a state $s_i$ in a model $\mathcal{M}$.

1. $\langle \mathcal{M}, s_i \rangle \models p$ iff $p \in L(s_i)$, for atomic $p$.
2. $\langle \mathcal{M}, s_i \rangle \models \neg A$ iff $\langle \mathcal{M}, s_i \rangle \not\models A$
3. $\langle \mathcal{M}, s_i \rangle \models A \land B$ iff $\langle \mathcal{M}, s_i \rangle \models A$ and $\langle \mathcal{M}, s_i \rangle \models B$
4. $\langle \mathcal{M}, s_i \rangle \models A \lor B$ iff $\langle \mathcal{M}, s_i \rangle \models A$ or $\langle \mathcal{M}, s_i \rangle \models B$
5. $\langle \mathcal{M}, s_i \rangle \models A \Rightarrow B$ iff $\langle \mathcal{M}, s_i \rangle \not\models A$ or $\langle \mathcal{M}, s_i \rangle \models B$
6. $\langle \mathcal{M}, s_i \rangle \models AB$ iff for each $\chi_{s_i}, \langle \mathcal{M}, \chi_{s_i} \rangle \models B$.
7. $\langle \mathcal{M}, s_i \rangle \models EB$ iff there exists $\chi_{s_i}$ such that $\langle \mathcal{M}, \chi_{s_i} \rangle \models B$.
8. $\langle \mathcal{M}, \chi_{s_i} \rangle \models B$ iff for each $s_j \in \chi_{s_i}$, if $i \leq j$ then $\langle \mathcal{M}, Suf(\chi_{s_i}, s_j) \rangle \models B$.
9. $\langle \mathcal{M}, \chi_{s_i} \rangle \models \Diamond B$ iff there exists $s_j \in \chi_{s_i}$ such that $i \leq j$ and $\langle \mathcal{M}, Suf(\chi_{s_i}, s_j) \rangle \models B$.
10. $\langle \mathcal{M}, \chi_{s_i} \rangle \models \Box B$ iff $\langle \mathcal{M}, Suf(\chi_{s_i}, s_{i+1}) \rangle \models B$.

In the SNF<sub>CTL</sub> these operators are defined via the basic set of SNF<sub>CTL</sub> operators [9].

**Definition 5 (Satisfiability)** An SNF<sub>CTL</sub> clause, $C$, is satisfiable if, and only if, there exists a model $\mathcal{M}$ such that $\langle \mathcal{M}, s_0 \rangle \models C$.

**Definition 6 (Validity)** An SNF<sub>CTL</sub> clause, $C$, is valid if, and only if, it is satisfied in every possible model.

The natural intuition behind SNF<sub>CTL</sub> is that the initial clauses provide starting conditions while step and sometime clauses constrain the future behaviour. An initial SNF<sub>CTL</sub> clause, start $\Rightarrow F$, is understood as “$F$ is satisfied at the initial state of some model $\mathcal{M}$”. Any other SNF<sub>CTL</sub> clause is interpreted taking also into account that it occurs in the scope of $A\Box$.

![Figure 2: Interpretation of step and sometime clauses.](image)

Thus, a clause $A\Box(x \Rightarrow A\Diamond p)$ (see Figure 2) is interpreted as “for any fullpath $\chi$ and any state $s_i \in \chi$ ($0 \leq i$), if $x$ is satisfied at a state $s_i$ then means that $p$ must be satisfied at the moment, next to $s_i$, along each path which starts from $s_i$”.

Next, a clause $A\Box(x \Rightarrow E\Diamond q_{(ind)})$ (a model for which is given again in Figure 2) is interpreted as “for any fullpath $\chi$ and any state $s_i \in \chi$ ($0 \leq i$), if $x$ is satisfied at a state $s_i$ then means that $q$ must be satisfied at the moment, next to $s_i$, along a path which starts from $s_i$ and which is associated with $\text{ind}$”. Speaking informally, we interpret $A\Box(x \Rightarrow E\Diamond q_{(ind)})$ such that given a state in a model which satisfies $x$ (the left hand side of the clause), the label, $\text{ind}$, indicates the direction, in which the successor state which satisfies $q$ can be reached (see similar developments in the construction of logic $\text{DCTL}^*$ [28]).

Finally, the labelling of the $E$ sometime clause is justified based upon its fixpoint characterization. Consider $A\Box(x \Rightarrow E\Diamond p_{(LC(ind))})$. This has the following meaning “for any fullpath $\chi$ and any state $s_i \in \chi$ ($0 \leq i$), if $x$ is satisfied at a state $s_i$ then $p$ must be satisfied at some state, say $s_j$ ($i \leq j$), along some path $\alpha_{s_i}$ which is the limit
As an example let us consider the following set of SNF/CTL clauses.

1. \( \text{start} \Rightarrow x \)
2. \( \text{start} \Rightarrow y \)
3. \( \text{start} \Rightarrow p \)
4. \( x \Rightarrow E \bigcirc x(t) \)
5. \( y \Rightarrow A \bigcirc \neg p \)
6. \( \text{true} \Rightarrow A \bigcirc (\neg x \lor p) \)

It is easy to establish that the given set of SNF/CTL clauses is unsatisfiable. Indeed, clauses 1 and 4 ensure that \( x \) is satisfied at every state along a fullpath labeled by \( f \). Let us consider this fullpath. Taking also into account clauses 3 and 6, we derive that \( p \) must be true at every state along the considered fullpath. At the same time, from 2 and 5 we conclude that \( \neg p \) must be satisfied at least at one state along any path of the model hence we have a contradiction. This proves that the set of Formulae above are unsatisfiable.

Note that in the full ECTL+ language the standard ‘until’ \( U \) and ‘unless’ \( W \) operators are used:

\[
\langle M, \chi_s \rangle \models A U B \quad \text{iff} \quad \text{there exists } s_j \in \chi_s \text{ such that } i \leq j \text{ and } \langle M, S u f (\chi_s, s_j) \rangle \models B \text{ and for each } s_k \in \chi_s, \text{ if } i \leq k < j \text{ then } \langle M, S u f (\chi_s, s_k) \rangle \models A.
\]

For example, the following rules can be applied to remove the \( W \) operator in the scope of either of the path quantifiers [9] where \( x \) is a new proposition:

**Removal of \( E \ W \)**

\[
\begin{align*}
P & \Rightarrow E(p \ W q)_{(LC\text{(ind))}} \\
P & \Rightarrow q \lor (p \land x) \\
x & \Rightarrow E \bigcirc (q \lor (p \land x))_{(ind)}
\end{align*}
\]

**Removal of \( A \ W \)**

\[
\begin{align*}
P & \Rightarrow A(p \ W q) \\
P & \Rightarrow q \lor (p \land x) \\
x & \Rightarrow E \bigcirc (q \lor (p \land x))
\end{align*}
\]

### 3.4 Example Specification

Let us consider a simple printing queue component model which consists of a client and one printing queue component as primitives. The client interfaces of the client are of type \( CI_c \) and the server interfaces of the printing queue are of type \( SI_r \). Finally, we have a simplified version of a life-cycle controller that allows to safely add or remove a binding between a client and the printing queue.

**Formal specification of non-functional aspects.** In order to allow for reconfiguration, not only the scenario must be formally specified, but also everything else which allows dynamic reconfiguration. Although in the fractal model four controller interfaces are defined, for reasons of space, we will only specify the safe-unbinding part of a reduced Life-Cycle Controller (LCC) so that it can be used in the deductive reasoning. Note that it is always possible to create new controllers if needed, in this case an appropriate set of formal specifications for each controller must be provided using a similar procedure. If a controller follows the standard Fractal model, a standard set of general temporal logic rules can be called and then modified to match the specification; otherwise, in the case of user-made definitions, the programmers themselves must provide the rules matching the criteria followed in the creation of the definition.

Next we will let the propositions \( \text{Bound}_1, \ldots, \text{Bound}_n \) denote the bindings between components. The format that each may take is \( \text{Bound}_i(CI_c, SI_r) \) \((1 \leq i \leq n)\) which is a proposition that (when true) specifies that a component with Client Interface \( CI_c \) is bound to the Server Interface \( SI_r \). In this example we have two primitive components, one for the Printing Queue and one for the Client using the Printing Queue. We would add as many of these propositions as necessary to describe the system.

\( \text{LCC} \) is a proposition which when true signifies that the Life Cycle Controller is active.

Before introducing the Life Cycle Controller Formula we would need to specify how components are started and stopped. However, for illustration in the context of this paper we will only provide a partial specification of the Life Cycle Controller and two primitive components; we only deal with the formula that captures the bindings of the two components. We will model the start of the components by attaching them to \( \text{start} \) .
Now we introduce the formula for our version of the Simplified Life-Cycle Controller:

\[ \neg LCC \land \neg (\text{Bound}_1(CI_a, SI_r) \lor \text{Bound}_2(CI_a, SI_r)) \Rightarrow A \square LCC \Rightarrow (\text{Bound}_1(CI_a, SI_r) \land \text{Bound}_2(CI_a, SI_r)) \]

which states that if neither of the components are bound and the LCC is not active then in all possible computations when the LCC is active then we must have the two components bound.

In the following example the Client can send a request for printing: \( req(CI_a) \) abbreviated below as \( req \). When true, this proposition states that a printing request has been raised by the client which possesses the client interface \( CI_a \). Similarly \( print \) is a proposition stating that a printing request has been satisfied by the printer.

**Formal specification of reconfiguration scenarios.**

For this section, we consider a simple printing queue component model (see figure 3) which consists of one client and one printing queue component as primitives. The client interface of the client is labelled \( CI_a \), and the server interfaces of the printing queue is labelled \( SI_r \). We will also consider a simplified life-cycle controller \( LCC \) that allows us to safely remove a binding between a client and the printing queue. This simple example is sufficient to demonstrate the potential of deductive reasoning, applied to a fractal model.

We will take in consideration the safety part of the specification and its requirements [30]. The Life-Cycle Controller \( LCC \) does not have a set specification being a non-functional component. We suggest that the system has a common protocol of communication (both Client and Printing Queue must follow a common process when a request is raised).

**Client specification:**

<table>
<thead>
<tr>
<th>Step</th>
<th>Proposition</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>( req \Rightarrow A(req \cup (req \land print)) )</td>
<td>Request is kept until it is possible to execute it</td>
</tr>
<tr>
<td>2</td>
<td>( req \Rightarrow A(\neg req2 \cup print) )</td>
<td>There will be no other request until job is printed</td>
</tr>
<tr>
<td>3</td>
<td>( req \Rightarrow A \Diamond \neg req )</td>
<td>The request for print will be eventually released</td>
</tr>
</tbody>
</table>

The complete specification of the primitive:

\[ \text{start} \Rightarrow \neg req \land (1) \land (2) \land (3) \]
where \( \lnot \text{req} \) defines the initial state for Client primitive.

**Printing queue specification:**

<table>
<thead>
<tr>
<th>Expression</th>
<th>Interpretation</th>
</tr>
</thead>
<tbody>
<tr>
<td>(4) ( A \square \lnot (\text{print} \land \text{print2}) )</td>
<td>Mutual Exclusion property: at every point in time, the printer can perform at most one printing operation:</td>
</tr>
<tr>
<td>(5) ( A \lnot \text{print} \lor \text{req} )</td>
<td>There is no printing unless requested</td>
</tr>
<tr>
<td>(6) ( \text{print} \Rightarrow A \Diamond \lnot \text{print} )</td>
<td>Printing will eventually end</td>
</tr>
<tr>
<td>(7) ( \text{req} \Rightarrow A \Diamond \text{print} )</td>
<td>The request for printing should be granted</td>
</tr>
</tbody>
</table>

The complete specification of the primitive:

\[
\text{start} \Rightarrow \lnot \text{print} \land (4) \land (5) \land (6) \land (7)
\]

Finally we specify the Life-Cycle Controller properties which affect the receiving of a printing request and the printing itself:

\[
\text{start} \Rightarrow [(\lnot \text{LCC} \land \lnot (\text{req} \lor \text{print})) \Rightarrow A \square (\text{LCC} \Rightarrow (\text{req} \land \text{print})))]
\]

When the life-cycle controller is activated, it ensures that Client Interface and Server Interface are bound, therefore allowing for requests to be sent from the Client, and prints to be carried out by the Printing Queue, for the specific binding.

We believe that the branching-time framework is appropriate for our specification targets because of the following reasons. Assume that after unbinding a client CI, it has been removed forever. Now, from this moment of time it is true to say that \( A \square \lnot \text{req} \) (in all possible futures from now on, there will be no more requests from the Client Interface to the Server Interface) and therefore at the previous moment of time it was true to say that \( E \Diamond A \square \lnot \text{req} \) (in some future it will not be possible for the Client interface to send a request to the Server Interface). The branching-time framework used shows how significant its use can be even in such simple example.

To apply deductive reasoning to this model, various properties could be taken into consideration. As a relatively simple example we consider the following property. Let \( p \) stands for \( \lnot \text{req} \land \lnot \text{print} \). Assume now that during the reconfiguration of the system the following property should be verified:

\[
\text{\( \Downarrow \) A} (\square (p \land \Diamond \lnot p))
\]

In the next section we will show how this formula can be represented in terms of \( \text{SNF}_{\text{CTL}} \) and then apply to this specification the resolution technique as a verification method.

## 4 The Verification Method - Clausal Temporal Resolution

### 4.1 Temporal Resolution Method for Branching-Time Logics

In order to achieve a refutation of the generated specification, we incorporate two types of resolution rules already defined in [9, 15]: *step resolution* (SRES) and *temporal* resolution (TRES).

**Step Resolution Rules.** Step resolution is used between Formulae that refer to the same initial moment of time or *same* next moment along some or all paths. In the formulation of the SRES rules below \( l \) is a literal and \( C \) and \( D \) are disjunctions of literals. Two step resolution rules that will be used in our example are given below.

**SRES 1**

\[
\begin{align*}
\text{start} & \Rightarrow C \lor l \\
\text{start} & \Rightarrow D \lor \lnot l \\
\text{start} & \Rightarrow C \lor D
\end{align*}
\]

**SRES 3**

\[
\begin{align*}
P & \Rightarrow A \Diamond (C \lor l) \\
Q & \Rightarrow E \Diamond (D \lor \lnot l) \tag{ind} \\
(P \land Q) & \Rightarrow E \Diamond (C \lor D) \tag{ind}
\end{align*}
\]
When an empty constraint is generated on the right hand side of the conclusion of the resolution rule, we introduce a constant false to indicate this situation and, for example, the conclusion of the SRES 1 rule, when resolving \( \text{start} \implies l \) and \( \text{start} \implies \neg l \), will be \( \text{start} \implies \text{false} \), which is the terminating clause.

**Temporal Resolution Rules.** In the rules below \( l \) is a literal and the first premises in the TRES rules abbreviate the \( A \) and \( E \) loops in \( l \) [14], i.e. the situation where, given that \( P \) is satisfied at some point of time, \( l \) occurs always from that point on all or some path respectively. Again, here we present only two temporal resolution rules that will be used in our verification example.

\[
\begin{align*}
\text{TRES 2} & \quad P \rightarrow A \bigcirc A \bigcirc l \\
& \quad Q \rightarrow E \bigcirc \neg l_{(LC \langle \text{ind} \rangle)} \\
& \quad Q \rightarrow E(\neg P \bigcirc \neg l)_{(LC \langle \text{ind} \rangle)} \\
\text{TRES 3} & \quad P \rightarrow E \bigcirc E \bigcirc l_{(LC \langle \text{ind} \rangle)} \\
& \quad Q \rightarrow A \bigcirc \neg l \\
& \quad Q \rightarrow A(\neg P \bigcirc \neg l)
\end{align*}
\]

### 4.2 Example Verification

To verify (‡) we apply the resolution method to the set of SNF\(_{CTL}\) clauses SNF\(_{CTL}(‡)\). We commence the resolution proof presenting at steps 1 – 13 the clauses of SNF\(_{CTL}(‡)\) in the following order: initial clauses, step clauses and, finally, any sometime clauses.

1. \( \text{start} \implies x \) 
2. \( \text{start} \implies \neg x \lor y \) 
3. \( \text{start} \implies \neg x \lor x_1 \) 
4. \( \text{start} \implies \neg z \lor \neg p \) 
5. \( \text{start} \implies \neg z \lor z_1 \) 
6. \( \text{true} \implies A \bigcirc (\neg z \lor \neg p) \) 
7. \( \text{true} \implies A \bigcirc (\neg z \lor z_1) \) 
8. \( x_1 \implies A \bigcirc y \) 
9. \( x_1 \implies A \bigcirc x_1 \) 
10. \( z_1 \implies E \bigcirc \neg p(t) \) 
11. \( z_1 \implies E \bigcirc z_1(t) \) 
12. \( y \implies A \bigcirc p \) 
13. \( x \implies E \bigcirc z_{(LC(t))} \) 
14. \( \text{start} \implies y \) 
15. \( \text{start} \implies x_1 \) 
16. \( y \implies A(\neg z_1 \lor p) \) 
17. \( y \implies p \lor \neg z_1 \land v \) 
18. \( v \implies A \bigcirc (p \lor \neg z_1 \land v) \) 
19. \( \text{start} \implies \neg y \lor p \lor \neg z_1 \land v \) 
20. \( \text{true} \implies A \bigcirc (\neg y \lor p \lor \neg z_1 \land v) \) 
21. \( \text{start} \implies p \lor \neg z_1 \) 
22. \( \text{start} \implies p \lor \neg z \) 
23. \( \text{start} \implies \neg z \) 
24. \( x_1 \implies A \bigcirc (p \lor \neg z_1) \) 
25. \( x_1 \implies A \bigcirc (p \lor \neg z) \) 
26. \( x_1 \implies A \bigcirc \neg z \)

We apply step resolution rules between 1 and 2, and 1 and 3. No more SRES rules are applicable. Formula 12 is an eventuality clause, and therefore, we are looking for a loop in \( \neg p \) (see [14] for the formulation of the loop searching procedure). The desired loop, \( E \bigcirc E \bigcirc \neg p(t)_{(LC(t))} \) (given that condition \( z_1 \) is satisfied) can be found considering clauses 10 and 11. Thus, we apply the TRES 3 rule to resolve this loop and clause 12, obtaining 16. Next we remove \( E \bigcirc W \) from 16 deriving a purely classical Formula 17 (\( y \) is a new variable). Simplify the latter, apply TEMP (the 'temporising' rule, see [9], obtaining, in particular, 19 and 20, and then a series of SRES rules to newly generated clauses.

14. \( \text{start} \implies y \) 
15. \( \text{start} \implies x_1 \) 
16. \( y \implies A(\neg z_1 \lor p) \) 
17. \( y \implies p \lor \neg z_1 \land v \) 
18. \( v \implies A \bigcirc (p \lor \neg z_1 \land v) \) 
19. \( \text{start} \implies \neg y \lor p \lor \neg z_1 \land v \) 
20. \( \text{true} \implies A \bigcirc (\neg y \lor p \lor \neg z_1 \land v) \) 
21. \( \text{start} \implies p \lor \neg z_1 \) 
22. \( \text{start} \implies p \lor \neg z \) 
23. \( \text{start} \implies \neg z \) 
24. \( x_1 \implies A \bigcirc (p \lor \neg z_1) \) 
25. \( x_1 \implies A \bigcirc (p \lor \neg z) \) 
26. \( x_1 \implies A \bigcirc \neg z \)

Now, as no more SRES rules are applicable, we find another eventuality, Formula 13, and thus we next look for a loop in \( \neg z \). This loop can be found considering Formulae 9 and 26: \( A \bigcirc A \bigcirc \neg z \) given that condition \( x_1 \) is satisfied. Thus, we can apply TRES 2 to resolve this loop and 13 deriving 27. Then we remove \( E \bigcirc W \) from the latter (on step 28, where \( w \) is a new variable, we use only one of its conclusions). Applying simplification and temporising to 28 we obtain 29. The desired terminating clause \( \text{start} \implies \text{false} \) is deduced by applying SRES 1 to steps 1, 15 and 23.
27. \[ x \Rightarrow E(\neg x_1 \, W \, z)_{(LC(f))} \, 9, 26, 13 \, TRES \, 2 \]
28. \[ x \Rightarrow z \vee \neg x_1 \wedge w \, 27 \, E \, W \, \text{Removal} \]
29. \[ \text{start} \Rightarrow \neg x \vee z \vee \neg x_1 \, 28 \, \text{SIMP, TEMP} \]
30. \[ \text{start} \Rightarrow \text{false} \, 1, 15, 23 \, \text{SRES \, 1} \]

We have found a contradiction, meaning that \( \text{SNF}_{\text{CTL}}(\dagger) \), hence \( \dagger \) itself is unsatisfiable.

5 Conclusions and Future Work

As we mentioned, there are two major approaches to formal specification and verification of distributed systems: explorative and deductive. To the best of our knowledge the only automated technique currently used in the verification of distributed hierarchical components is model checking. In this paper we have introduced a formal framework for the deductive verification of modular specification. As a specification tool we use the branching-time temporal logic. Specified properties and requirements of the system are then translated into the language of a normal form, \( \text{SNF}_{\text{CTL}} \), thus enabling the application of a powerful resolution method. An obvious benefit of this approach is avoiding the construction of a finite model (needed for the model checking).

Future extensions of this work will be in the application of the Inferential Erotetic Logic (IEL) tools aiming at optimisation of the process of reconfiguration of a component model.

References


